THINK ACADEMY

MATH CLASSES By O.P. GUPTA

CLICK HERE

VISHWAS TEST SERIES - 8
(For Academic session 2024-25)

Max. Marks - 30

Time - 60 Minutes

Class XI - Mathematics (041) Topics - Sequences & Series

Followings are of 2 Marks each (Q01-05).

Q01. Evaluate:
$$\sum_{r=2}^{10} (3+2^{2r})$$
.

- Q02. Prove that the sum of n arithmetic means between any two numbers is n times the single arithmetic mean between them.
- Q03. For what value of n, $\frac{a^{n+1}+b^{n+1}}{a^n+b^n}$ is the arithmetic mean of a and b?
- Q04. Sum of terms of an infinite geometric progression is 15 and the sum of the squares of these terms is 45. Deduce the progression.
- Q05. Let $x = 1 + a + a^2 + ...$ and $y = 1 + b + b^2 + ...$ where |a| < 1, |b| < 1. Then, prove that : $1 + ab + a^2b^2 + ... = \frac{xy}{x + y - 1}$. $[2 \times 5 = 10]$

Followings are of 3 Marks each (Q06-07).

- Q06. If a, b, c are in G.P. and x be the A.M. between a, b and y be the A.M. between b, c respectively, then show that $\frac{a}{x} + \frac{c}{y} = 2$.
- Q07. Prove that $P^2 = \left(\frac{S}{R}\right)^n$ where S be the sum, P the product and R the sum of reciprocals of n terms in a geometric progression.

OR

Evaluate: 5+55+555+555+... upto n terms.

 $[3 \times 2 = 6]$

Following is of 4 Marks (Q08).

Q08. **PASSAGE BASED QUESTION**: Let $G_1, G_2, G_3, ..., G_n$ be n G.M.'s between a and b.

Then $a, G_1, G_2, G_3, ..., G_n$, b are in G.P. Here 'b' is the $(n+2)^{th}$ term i.e., $b = a r^{(n+2)-1} = a r^{n+1}$.

This gives,
$$r = \left(\frac{b}{a}\right)^{\frac{1}{n+1}}$$
.

Thus first G.M. means 2^{nd} term of the G.P. i.e., $G_1 = a r = a \left(\frac{b}{a}\right)^{\frac{1}{n+1}}$; second G.M. means 3^{rd} term of the

G.P. i.e.,
$$G_2 = a r^2 = a \left(\frac{b}{a}\right)^{\frac{2}{n+1}}$$
 and so on.

Hence, nth G.M. between a and b is given as, $G_n = a r^n = a \left(\frac{b}{a}\right)^{\frac{n}{n+1}}$.

Based on the above information, answer the following questions.

- (a) Insert four geometric means between 5 and 160.
- **(b)** Find the value of k, such that $\frac{a^{k+1} + b^{k+1}}{a^k + b^k}$ represents the single geometric mean between positive numbers a and b. $[2 \times 2 = 4]$

Followings are of 5 Marks each (Q09-10).

Q09. The ratio of A.M. and G.M. of two positive numbers a and b is m: n. Deduce a: b.

OR

Sum of three numbers in G.P. is 56. If we subtract 1, 7, 21 from these numbers in that order, we obtain an A.P. Find these numbers.

Q10. If p, q, r are in the geometric progression and the equations, $px^2 + 2qx + r = 0$ and $dx^2 + 2ex + f = 0$ have a common root, then show that $\frac{d}{p}$, $\frac{e}{q}$, $\frac{f}{r}$ are in arithmetic progression. [5×2=10]



We have released Set of **2 Books** for CBSE Class XI (Academic session 2024-25).

1. MATHMISSION FOR XI

☑ COMPLETE THEORY & EXAMPLES☑ SUBJECTIVE TYPE QUESTIONS☑ COMPETENCY FOCUSED QUESTIONS

- ♠ Multiple Choice Questions
- ❖ Assertion-Reason Questions
- **♦** Case-Study Questions
- ❖ Passage-Based Questions
- ☑ ANSWERS OF ALL QUESTIONS

2. SOLUTIONS OF MATHMISSION

☑ Step-by-step Detailed Solutions (For all Exercises of MATHMISSION)

• You can **Share this document** with other students.

₩ith a lot of Blessings!

O.P. GUPTA

Author & Math Mentor Indira Award Winner

The O.P. Gupta Advanced Math Classes @ Think Academy, Near Dhansa Bus Stand Metro Station Gate No.3, Najafgarh, Delhi

© Telegram / WhatsApp : +919650350480

YouTube.com/@theopgupta

Exclusive coaching for Maths (041)

By O.P. GUPTA

☑ CBSE XII

☑ CBSE XI

☑ CUET

☑ JEE - MAIN

☑ NDA

Grab the best Seller book for X, XI & XII Maths (041) CBSE Exams.

☑ MATHMISSION FOR XII, XI & X

(Refresher Guide with Competency Focused Questions)
♣ These books are developed as per CBSE curriculum for 2024-25.

☑ CBSE 21 SAMPLE PAPERS FOR XII

- ☑ CBSE YODDHA SAMPLE PAPERS FOR XI
- ☑ CBSE UMANG SAMPLE PAPERS FOR X
- ☑ NTA CUET (UG) QUESTION BANK IN MATHS

(Order now at Discounted rate on WhatsApp - 9650350480)



MATHEMATICIA BY O.P. GUPTA

...a name you can bank upon!



Feel Safe to **Share this Document** with other math scholars

CLICK NOW

TO

Download



or, just type theopgupta.com

FREE PDF TESTS AND ASSIGNMENTS OF THE CLASSES XII, XI & X



To get FREE PDF Materials, join **WhatsApp Teachers Group** by Clicking on the Logo

Click on the **Book cover** to buv!



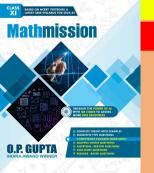
If you are a Student, then you may join our Students Group



CLICK HERE FOR **CLASSES** XI & XII

You can add our WhatsApp no. +919650350480 to your Groups also

Many Direct Questions from our Books have been asked in the recent CBSE Exams





2024-25 Edition

Buv our books on









amazon

For Bulk Orders of our Books at Discounted Price, contact on +91-9650350480

Flipkart